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Math 2243,
March 24, 2004
There are 4 partial credit questions, each of them worth 25 points. NO GRAPHIC CALCULATORS are permitted. GOOD LUCK !

1. Answer both of the following two questions :
a) Give an example of two square matrices $A$ and $B$ such that $A B \neq B A$
b) Find a nonzero matrix(a matrix for which not all the entries are zero) that satisfies the equality $A^{2}=0$.
2. Let $V=\left\{(x, y, z) \in R^{3} \mid x+y-z=0\right\}$. Find an orthonormal basis in $V$.
3. Consider the following subset of $R^{3}$

$$
S=\left\{(x, y, z) \in R^{3} \mid y^{2}-x z=0\right\}
$$

Is $S$ a vector subspace of $R^{3}$ ? What is the span of this subset?
4. Let $f(t)=t, \quad g(t)=e^{t}$ and $h(t)=t^{3}$. Are these three functions linearly independent? Is $l(t)=t^{2}$ in the subspace generated by $f, g$ and $h$ ?

